

PARCHMENT GLUTAMINE INDEX (PQI): A NOVEL METHOD TO ESTIMATE GLUTAMINE DEAMIDATION LEVELS IN PARCHMENT COLLAGEN OBTAINED FROM LOW-QUALITY MALDI-TOF DATA

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85 **ABSTRACT**

86 Parchment was used as a writing material in the Middle Ages and was made using animal
87 skins by liming them with $\text{Ca}(\text{OH})_2$. During liming, collagen peptides containing Glutamine
88 (Q) undergo deamidation resulting in a mass shift of 0.984 Da. Assessing the extent of deami-
89 dation can inform us about parchment production patterns and quality. In this study, we
90 propose a simple three-step workflow, developed as an R package called `MALDIpqi()`, to esti-
91 mate deamidation in parchment derived collagen using low-resolution MALDI spectra. After
92 pre-processing raw spectra, we used weighted least-squares linear regression to estimate Q
93 deamidation levels from the convoluted isotopic envelope for seven collagen-peptide markers.
94 Finally, we employed a linear mixed effect model to predict the overall deamidation level of
95 a parchment sample termed Parchment Glutamine Index (PQI). To test the robustness of
96 the workflow, we applied `MALDIpqi()` to previously published ZooMS data generated from
97 almost an entire library of the Cistercian monastery at Orval Abbey, Belgium. In addition
98 to reliably predicting PQI, we observed interesting patterns pertaining to parchment pro-
99 duction. `MALDIpqi()` holds excellent potential for biocodological and other archaeological
100 studies involving collagen, such as bone, but we also foresee its application in the food and
101 biomedical industry.

102 **INTRODUCTION**

103 Glutaminyl and asparaginyl residues are molecular clocks which deamidate with predeter-
104 mined half-lives [Robinson et al., 2006]. Glutamine (Gln, Q) deamidation occurs via two
105 mechanisms, 1) direct hydrolysis, and 2) through the formation of a cyclic imide interme-
106 diate. Irrespective of the mechanism, instability of reaction intermediates results in slower
107 deamidation rates of Gln. Because the deamidation rates of glutaminyl residues are slower
108 than asparaginyl residues [Robinson et al., 2004, Wright, 1991], it has been advanced that
109 Gln deamidation could be a better tool at our disposal to investigate chemical processes such
110 as assessing the quality of skins in the food and leather industries [Maffia et al., 2004] and
111 the age of fossils [van Doorn et al., 2012, Wilson et al., 2012], although in the latter case
112 [Schroeter and Cleland, 2016] argue that Gln deamidation is an indicator of preservational
113 quality and environmental conditions rather than age (and authenticity) of ancient proteins.
114 Here, we use Gln deamidation to assess variability in parchment production.

115 Mass spectrometry is well suited to detecting sites of deamidation, which increases the
116 molecular weight of deamidated peptide molecules by 0.984 Dalton (Da). This is easily
117 detected and localised in the sequence by a mass shift in MS2 spectra. However, in MS1, the
118 similarity in mass gain with that of a neutron (1.007 Da) means that the deamidated and
119 non-deamidated isotopic envelopes overlap.

120 We explore a mathematical approach to derive the level of deamidation in glutamine
121 from MS1 data from peptide mass fingerprinting of collagen. We use an isotopic envelope
122 deconvolution method (similar to the approach used by Wilson et al., 2012) to estimate the
123 extent of glutamine deamidation in selected tryptic peptides but then integrate the individual
124 deamidation estimates to derive an overall index for a given sample. In order to develop the
125 method we have used published MALDI spectra of parchment (e.g. [Fiddymment et al., 2015])
126 which we have then applied to a newly released data set from Orval Abbey [Ruffini-Ronzani
127 et al., 2021].

128 Parchment is the dehaired and limed skin of an animal [Reed, 1972, Ryder, 1964]. Liming

129 is typically the first stage in parchment and leather preparation, it loosens the hairs from
130 the hides, swells the collagen and saponifies some of the skin lipids prior. Gln deamidation
131 occurs when the skins are soaked in lime, a solution of calcium hydroxide $\text{Ca}(\text{OH})_2$, which
132 at ambient temperature has an average pH of about 12.4 and is used in different strengths
133 during the parchment making process. The alkaline environment results in direct side chain
134 hydrolysis of the amide group on asparagines and glutamines. A longer exposure (or higher
135 concentration and/or temperature) of lime results in an increase in the extent of deamida-
136 tion. If not controlled correctly, an excessive exposure to lime can compromise the integrity
137 of skin and to weaken it to such a degree that is no longer usable. By measuring the level of
138 deamidation present in different samples we can start to assess the different production qual-
139 ities from different regions and time and correlate this to prices and availability of parchment
140 obtained from historic records. Consequently, the extent to which these skins are limed can
141 be interrogated through the measurement of the level of glutamine deamidation.

142 By assessing the relative rates of deamidation of different tryptic peptides we derived a
143 single value (with associated errors) which we term the Parchment Glutamine Index (PQI).
144 Samples which retain the most intact glutaminy residues have the highest PQI values; as
145 deamidation increases, PQI falls. In MALDI-TOF mass spectrometry baseline noise in the
146 spectra [Kolibal and Howard, 2006, Krutchinsky and Chait, 2002] results in a distortion of
147 the relative intensity of the peaks across an isotope envelope which in turn affects estimates
148 of deamidation based on the deconvolution of the envelope. Consequently values greater than
149 1 (ie. no deamidation) are possible due to noisy baselines, while values close to 0 are never
150 observed in parchment, as this would follow complete gelatinisation.

151 **MATERIALS**

152 In order to establish the model, we used available published ZooMS [Buckley et al., 2009]
153 data to establish correlations between the rates of deamidation of different tryptic peptides.
154 We then test our model using data generated from almost the entire library of the Cisterian
155 monastery at Orval Abbey, Belgium [Ruffini-Ronzani et al., 2021]. Explanation of the data

156 generated can be found in the data article [Bethencourt et al., 2022] and the ZooMS data is
157 uploaded in Zenodo (<https://doi.org/10.5281/zenodo.5648106>).

158 **METHODS**

159 **4.1 Selection of peptides**

160 In order to assess the overall PQI we used as many peptides as possible and selected them
161 based upon the following criteria:

- 162 1. They contain at least one glutamine.
- 163 2. They are consistently and reliably detected in the MALDI-TOF MS analysis.
- 164 3. They are present in all three species used to make parchment (calf, sheep and goat).
165 All these peptides have the same mass in the different species, except m/z 3033 and
166 3093, which are the equivalent peptides for calf/sheep and goat, respectively.

167 A final list consisting of eight peptides was compiled (Table 1), of which a maximum of
168 seven can be detected in any one sample due to the equivalence of peptides m/z 3033 and
169 3093), and used to run the subsequent analysis.

170 **4.2 Pre-processing of raw data**

171 We performed pre-processing of the spectra using the R [R Core Team, 2021] package `MALDIquant`
172 [Gibb and Strimmer, 2012]:

- 173 • The Savitzky-Golay-filter [Savitzky and Golay, 1964] smoothed the spectra and reduced
174 small, highly frequent noise. This allows for better subsequent baseline and noise es-
175 timation and peak maxima determination. We used a moving half-window size of 8,
176 following the recommendation by [Bromba and Ziegler, 1981] of keeping it smaller than
177 the full width at half maximum of the peaks.
- 178 • We estimated the baseline (and then subtracted) using the Statistics-sensitive Non-
179 linear Iterative Peak-clipping algorithm (SNIP) [Ryan et al., 1988] implemented in
180 `MALDIquant`; the iterations parameter of the algorithm is set to 20.

- 181 • We estimated noise using the SuperSmoother [Friedman, 1984] method. Peaks are
182 detected if they are a maximum with a half-window size of 20 and are above a signal
183 to noise ratio of 1.5.
- 184 • Finally, we extracted isotopic-like distributions for each of the selected peptides by
185 finding the canonical m/z value and 5 following peaks (if detected) at the isotopic
186 distance of 1 Da, allowing for a small tolerance deviation of $1.5 \cdot 10^{-4} \cdot mass$ units.

187 Figure 2 shows the spectra before and after pre-processing for five randomly selected
188 samples.

189 4.3 Estimation of deamidation level of peptides

190 Deamidation of a peptide consisting of glutamine (Q) at a single site results in a mass shift of
191 approximately +0.984 Da so that the first peak of the isotope distribution for the deamidated
192 peptide coincides with the second peak of the isotope distribution for the non-deamidated
193 peptide (at the resolution of our data). For a peptide with k possible deamidation sites, each
194 additional deamidation results in a further +0.984 Da mass shift leading to k overlapping
195 isotope distributions. The level of deamidation of a peptide can be estimated by deconvoluting
196 the two overlapping isotopic distributions.

197 4.3.1 Theory

In order to explain the method, we focus on one peptide and assume there are $m + 1$ isotopic peaks of the peptide available with isotope distribution

$$I_i, \quad i = 0, \dots, m, \quad I_0 + I_1 + \dots + I_m = 1.$$

We followed the method as described in Wilson et al. [2012] to calculate theoretical isotopic distributions for the peptides. For convenience, we put $I_i = 0$ for $i < 0$. During deamidation, we expect a shift in the isotope distribution

$$P_i = \beta_0 I_i + \beta_1 I_{i-1} + \dots + \beta_k I_{i-k}, \quad i = 0, \dots, m,$$


198 where $1 \leq k < m$ and $\beta_\ell \geq 0$, $\ell = 0, \dots, k$, is the probability that ℓ positions are deamidated,
199 such that $\beta_0 + \beta_1 + \dots + \beta_k = 1$. It holds that $P_0 + P_1 + \dots + P_m = 1$. In the current study,
200 we take $k = 1$.

201 4.3.2 Weighted least square and linear regression

202 We developed a general theory assuming $m+1$ measurements, one for each isotope, replicated
203 n times. However, to estimate the overall deamidation level from multiple peptides and
204 replicates simultaneously (see Section 4.4) we obtained estimates of the deamidation level for
205 each of the 3 replicates separately, that is, we apply the theory below with $n = 1$.

Notation for observed intensities of each isotopic peak and replicate:

$$x_{ij}, \quad i = 0, \dots, m \text{ (isotopic peaks)}, \quad j = 1, \dots, n \text{ (replicates)}.$$

206  There might be missing values and/or missing replicates.

The measurements are proportional to P_i , $i = 0, \dots, m$, hence in particular the measurements do not sum to one. In general, consider the linear model

$$x_{ij} = \gamma_0 I_i + \gamma_1 I_{i-1} + \dots + \gamma_k I_{i-k} + \epsilon_{ij},$$

where $\gamma_\ell \geq 0$, $\ell = 0, \dots, k$, are parameters, and ϵ_{ij} is (unobserved) noise. The deamidation fractions are obtained as

$$\beta_\ell = \frac{\gamma_\ell}{\gamma_0 + \dots + \gamma_k}.$$

207 We avoided assuming a specific noise structure (for example, normal distributed noise)
208 and used weighted least square to estimate the unknown parameters,

$$\hat{\gamma} = (\hat{\gamma}_0, \dots, \hat{\gamma}_k) = \operatorname{argmin}_{\gamma, c} \sum_{j=1}^n \sum_{i=0}^m w_{ij} (x_{ij} - c_j X_i \gamma)^2, \quad (1)$$

where $\gamma = (\gamma_1, \dots, \gamma_k)^\top$ is a column vector and $c = (c_1, \dots, c_n)$ is a row vector. Here c_j is a scaling factor for the j 's replicate with $c_1 = 1$. The idea being that replicates show the same

trend but might vary in signal intensity, hence scaling is required to adjust the parameters.

Furthermore, w_{ij} is a weight for the x_{ij} 's data point, and X_i is the i th row of

$$X = \begin{pmatrix} I_0 & 0 & 0 & \dots & 0 \\ I_1 & I_0 & 0 & \dots & 0 \\ I_2 & I_1 & I_0 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ I_k & I_{k-1} & I_{k-2} & \dots & I_0 \\ I_{k+1} & I_k & I_{k-1} & \dots & I_1 \\ \vdots & \vdots & \vdots & & \vdots \\ I_m & I_{m-1} & I_{m-2} & \dots & I_{m-k} \end{pmatrix}.$$

209 In total there are $(k+1) + (n-1) = k+n$ parameters and $n(m+1)$ measurements, assuming
 210 none are missing. If measurements are missing the corresponding terms in Equation (1) are
 211 omitted.

The estimates can be obtained by weighted linear regression with design matrix X and diagonal weight matrix

$$W_j = \text{diag}(w_{0j}, w_{1j}, \dots, w_{mj}).$$

212 Let X_j^o be the matrix X with the rows corresponding to the missing measurements of replicate
 213 j omitted (upper index o for omitted), let W_j^o be the matrix W_j with the rows and columns
 214 corresponding to the missing measurements of replicate j omitted, and let x_j^o be the column
 215 vector with missing measurements or replicate j omitted.

216 Then the estimates can be obtained iteratively by

$$\hat{\gamma}^{i+1} = \left(\sum_{j=1}^n (\hat{c}_j^i)^2 (X_j^o)^T W_j^o X_j^o \right)^{-1} \sum_{j=1}^n \hat{c}_j^i (X_j^o)^T W_j^o x_j^o, \quad (2)$$

217 and

$$z_j^i = \frac{(W_j^o x_j^o)^T X_j^o \hat{\gamma}^i}{(W_j^o X_j^o \hat{\gamma}^i)^T X_j^o \hat{\gamma}^i}, \quad \hat{c}_j^i = \frac{z_j^i}{z_1^i + \dots + z_n^i}, \quad (3)$$

218 where $\hat{\gamma}^i$ and \hat{c}^i are the i th iterated estimates of the column vectors γ and $c = (c_1, \dots, c_n)$.
219 One continues until the difference between consecutive estimates is small with initial estimate
220 $\hat{c}^1 = (1, \dots, 1)$.

221 Equation (2) is the standard weighted least square estimate assuming the scaling factors
222 are known. Equation (3) is an update of the scaling factors assuming the other parameters
223 are known.

224 For use in the later stage of the workflow to estimate the overall deamidation level (see
225 Section 4.4.1) we define the *Reliability measure*

$$\text{Reliability} = \sum_{j=1}^n \sum_{i=0}^m w_{ij} (x_{ij} - \hat{c}_j X_i \hat{\gamma})^2 \quad (4)$$

226 If there is only one replicate ($n = 1$) or one estimates γ separately for each replicate, then

$$\hat{\gamma}^{(j)} = ((X_j^o)^T W_j^o X_j^o)^{-1} (X_j^o)^T W_j^o x_j^o, \quad (5)$$

227 and there is no need for iteration.

The weights might be chosen in different ways. Here, we assume the noise term on measurements is additive, so at the same level for each measurement. In that case, one might apply

$$w_{ij} = \frac{1}{n_{ij}}, \quad i = 0, \dots, m, \quad j = 1, \dots, n,$$

228 where n_{ij} is the estimated background noise for that particular measurement. Within one
229 replicate, n_{ij} is roughly of the same size for all $i = 0, \dots, m$, but differs between replicates.
230 Herein, we calculate the noise as explained in Section 4.2 using the SuperSmoother method
231 [Friedman, 1984].

232 4.3.3 Deamidation fractions

By normalisation

$$\hat{\beta}_\ell = \frac{\hat{\gamma}_\ell}{\hat{\gamma}_0 + \dots + \hat{\gamma}_k}$$

233 are estimates of the deamidation fractions corresponding to the parameters β_ℓ , $\ell = 0, \dots, k$,
234 in Section 4.3.1. In our application of the theory we take $k = 1$, and let q be the (least square
235 estimated) fraction of the remaining, undeamidated Q, i.e. $q = \hat{\beta}_0 = \frac{\hat{\gamma}_0}{\hat{\gamma}_0 + \hat{\gamma}_1}$. Herein, we
236 define the fraction of undeamidated Q (q) as the extent of deamidation with $q = 1$ meaning
237 no deamidation where as $q = 0$ referring to complete deamidation. Histograms of the extent
238 of deamidation (q) of eight peptides are shown in Supplementary figure 1.

239 **4.4 Estimation of the overall deamidation level**

240 We propose a linear mixed effect model, henceforth called the Parchment Glutamine Index
241 (PQI) model, that integrates the estimated values of q and their analytical reliability with
242 which the deamidation level is estimated. The Parchment Glutamine Index (PQI) model thus
243 predicts an overall level of deamidation in a sample and an associated error of prediction.

244 **4.4.1 PQI Model**

245 The (PQI) model is a linear mixed effect model (LMM) that considers log-transformed q val-
246 ues as response variable with individual Peptide as the fixed effects, and Sample and Replicate
247 as the random effects. As a result, the LMM fits the response variable at three different lev-
248 els, namely, i) peptide, ii) sample, and iii) replicate. Herein, we use log-transformed q as the
249 response variable to reflect the underlying kinetics of the loss of intact glutamine residues
250 which follows pseudo-first order kinetics. Hence, the PQI model predicts the log-transformed
251 deamidation level of a sample from the deamidation level of its individual peptides.

252 To simplify, we change the notation and structure of the data with respect to the previous
253 section. Herein, the dataset is structured with $\log(q)$ values, *Reliability* estimates (see Section
254 4.3.2), factors that identifies Peptide (P , with n_P levels), Sample (S , with n_S levels) and
255 Replicate (R , with n_R levels). A summary of the dataset is given in Table 2.

256 Let $t = 1, \dots, u$ denote the observation index, where u is the number of rows, and $u =$
257 $n_S \cdot n_R \cdot n_P$. The statistical model that we will use is the linear mixed effects model given by

$$\log(q_t) = \theta(P_t) + Y(S_t) + Z(S_t, R_t) + \epsilon_t \quad (6)$$

258 where,

- 259 • $\theta(P_1), \dots, \theta(P_{n_P})$ are the fixed effects of the each peptides,
- 260 • $Y(S) \sim \mathcal{N}(0, \sigma_S^2)$ and $Z(S, R) \sim \mathcal{N}(0, \sigma_R^2)$ are the random components from sample,
261 and replicate respectively, and
- 262 • $\epsilon_t \sim \mathcal{N}(0, (\text{Reliability}_t)^{2\mu} \cdot \sigma_{P_t}^2)$ are the residuals.

263 The variance parameters for random effects are σ_S^2 (sample, S) and σ_R^2 (replicate, R), and
264 for the fixed effects of each peptide are $\sigma_{P_1}^2, \dots, \sigma_{P_{n_P}}^2$. Furthermore, we scaled the residual
265 variances by *Reliability* values generated from weighted square linear regression, see Eq. (4),
266 to some power 2μ , and the PQI model estimates μ .

The aim is to predict $Y(s)$ given the observations of $\log(q_t)$ for indices t with $S_t = s$. $Y(s)$ is the random effect in the proposed linear mixed effect model that gives us the overall level of deamidation in a given sample, termed as PQI. To formalize this we define

$$J_s = \{t = 1, \dots, u : S_t = s\},$$

267 so that J_s are the set of observation indices belonging to sample s . Additionally, we will use
268 the following notation as given below:

- 269 • $|J_s|$ is the size of J_s ,
- 270 • M^\top is the transpose of a matrix M ,
- 271 • $\mathbf{1}_v$ is the column vector of length v consisting of 1's,
- 272 • $\delta_{x=y}$ is the Dirac delta taking the value 1 when $x = y$ and 0 otherwise,
- 273 • $\text{diag}(w)$ is the diagonal matrix with the vector w in the diagonal.

Using this notation we have

$$\begin{pmatrix} Y(s) \\ \{\log(q_t)\}_{t \in J_s} \end{pmatrix} \sim \mathcal{N} \left(\begin{pmatrix} 0 \\ \{\theta(P_t)\}_{t \in J_s} \end{pmatrix}, \begin{pmatrix} \sigma_S^2 & \sigma_S^2 \cdot \mathbf{1}_{|J_s|}^\top \\ \sigma_S^2 \cdot \mathbf{1}_{|J_s|} & \Xi \end{pmatrix} \right)$$

with $\Xi = \text{Var}(\{\log(q_t)\}_{t \in J_s}) \in \mathbb{R}^{|J_s| \times |J_s|}$ given by

$$\Xi = \sigma_S^2 \cdot \mathbf{1}_{|J_s|} \mathbf{1}_{|J_s|}^\top + \sigma_R^2 \cdot \{\delta_{R_p=R_q}\}_{p,q \in J_s} + \text{diag} \left(\{(\text{Reliability}_t)^{2\mu} \cdot \sigma_P^2\}_{t \in J_s} \right)$$

In particular, if we have observations of 3 replicates for all 7 peptides, then $\Xi \in \mathbb{R}^{21 \times 21}$ and it is given by

$$\sigma_S^2 \cdot \mathbf{1}_{21} \mathbf{1}_{21}^\top + \sigma_R^2 \cdot \mathbf{1}_3 \mathbf{1}_3^\top \otimes \text{diag}(\mathbf{1}_7) + \text{diag} \left(\{(\text{Reliability}_t)^{2\mu} \cdot \sigma_P^2\}_{t \in J_s} \right)$$

From the above joint normal distribution it follows by standard formulae that the conditional mean and the conditional variance of $Y(s)$ are given by

$$\begin{aligned} \mathbb{E}[Y(s) | \{\log(q_t)\}_{t \in J_s}] &= \sigma_S^2 \cdot \mathbf{1}_{|J_s|}^\top \Xi^{-1} (\{\log(q_t) - \theta(P_t)\}_{t \in J_s}), \\ \text{Var}[Y(s) | \{\log(q_t)\}_{t \in J_s}] &= \sigma_S^2 - \sigma_S^4 \cdot \mathbf{1}_{|J_s|}^\top \Xi^{-1} \mathbf{1}_{|J_s|} \end{aligned}$$

274 Note that $\mathbb{E}[Y(s) | \{\log(q_t)\}_{t \in J_s}]$ is the prediction of $Y(s)$, and $\text{Var}[Y(s) | \{\log(q_t)\}_{t \in J_s}]$ is
275 the associated prediction variance.

276 4.5 Analysis workflow

277 We performed all the computations in the statistical programming language R [R Core Team,
278 2021] using the following packages: `nlme`[Pinheiro et al., 2021], `dp1yr`[Wickham et al., 2021],
279 and `ggplot2`[Wickham, 2016]. The prediction of $Y(s)$ can be extracted directly from the
280 `lme`-object using the function `nlme::ranef()`. However, the computation of the predic-
281 tion variance requires implementation of the matrix formula. We developed an R package
282 `MALDIpqi` for the whole workflow consisting of pre-processing of raw spectra, estimation

283 of deamidation rates using weighted least squares linear regression, and applying linear
284 mixed effect model to estimate the overall deamidation index of parchment, available at
285 <https://github.com/ismaRP/MALDIpqj>.

286 **RESULTS AND DISCUSSION**

287 We applied the workflow starting from pre-processing of raw data followed by estimation of
288 deamidation levels of individual peptides and finally predicting the overall sample deamida-
289 tion level, termed as PQI.

290 We let q denote the fraction of remaining non-deamidated Q (see Section 4.3.3) in the
291 peptide under consideration. We estimated q values for selected eight peptides using weighted
292 least squares linear regression on the isotopic distribution as obtained from MALDI-TOF
293 spectra. Table 3 shows the first and third quartile of estimated q values to give an overview
294 of deamidation levels in the peptides.

295 **5.1 Relative rates of deamidation**

296 Assuming the deamidation level over time follows first-order kinetics (N. E. Robinson &
297 Robinson, 2004), then denoting the amount of non-deamidated Q of a particular peptide at
298 time t by $[Q]_t$, we have

$$[Q]_t = [Q]_0 e^{-kt}, \quad (7)$$

299 and hence

$$q = \frac{[Q]_t}{[Q]_0} = e^{-kt} \quad (8)$$

300 where, $[Q]_0$ is the amount of Q at time 0, k is the deamidation rate constant, and t is the
301 age of the sample.

302 Let k_1 and k_2 denote the deamidation rate constants of Peptide 1 and Peptide 2, respec-
303 tively, from a particular sample. Similarly, let q_1 and q_2 denote the deamidation fractions of
304 Peptide 1 and Peptide 2, respectively. Then the ratio of the deamidation rate constant of

305 Peptide 2 to that of Peptide 1 can be expressed as

$$\frac{k_2}{k_1} = \frac{\log(q_2)}{\log(q_1)}. \quad (9)$$

306 Considering Peptide 1 to deamidate slowly, we obtain a relative deamidation rate profile for
307 each sample that might be compared across samples. Using this ratio overcomes the need to
308 establish the absolute rate of deamidation. A limitation of this approach is when the levels
309 of deamidation are very high, the true extent may be obscured due to the correspondingly
310 high influence of noise in the spectra.

311 Among the eight peptides the rates (see Table 3) are compared relative to COL1 α 1 508-
312 519 (m/z 1105.58, VQG) which deamidates the most slowly. The only peptide which does not
313 have a Glycine (Gly) C-terminal to the Gln is peptide COL1 α 1 376-396 (m/z 2040.97, GQD),
314 and this is the most rapidly deamidated. This rapid deamidation explains the clustering of
315 fitted values towards the left of the residual plot for this peptide, as shown in Figure 4.
316 COL1 α 1 934-963 (m/z 2689.25), contains two glutamine residues both oriented in the same
317 plane (PQGFQG), but even their combined rate is nevertheless slower than COL1 α 1 376-
318 396. Curiously m/z 3084.42 (identified by Mascot [Perkins et al., 1999] as COL1 α 1 9-42)
319 has a rate of deamidation which is one third that of m/z 3116.40, which was interpreted as
320 the same peptide but with only two less oxygen atoms. The most probable explanation is
321 that one of these peptides may have been misidentified, as it seems unlikely that additional
322 oxidation/hydroxylations would have such a significant effect on the rate of deamidation.

323 The log-transformed q values were then transferred to the PQI model, which fits the
324 deamidation at peptide level and predicts the sample level deamidation. We used the `lme`
325 function in R from the package `nlme` to fit the linear mixed effect model using restricted
326 maximum likelihood (REML). PQI model estimates for sample level variance(σ_S^2) is 0.01 and
327 replicate level variance (σ_R^2) is $4.09 * 10^{-11}$ with $\mu = -0.06$. The back-transformed peptide
328 level fixed effect estimates $\exp(\hat{\theta})$ and the relative levels of deamidation are given in Table 3.

329 We validated the model fitting using residual plots (residuals vs. fitted values) and nor-

330 mal quantile-quantile plots of the Pearson residuals (residuals standardized by their estimated
331 standard deviation). Residual plots are the most common diagnostic tool to assess the con-
332 stant variation of residuals [Pinheiro and Bates, 2000]. Diagnostic plots for PQI model fitting
333 for the slowest deamidating peptide, COL1 α 1 508-519, are shown in Figure 3 showing a valid
334 statistical model except slightly too heavy tails in the normal distribution. Pearson residuals
335 for almost all samples are randomly distributed around 0 with magnitudes ranging between
336 ± 2 , and without any concerning patterns as depicted in Figure 4.

337 Normal quantile-quantile plots compare quantiles of Pearson residuals to quantiles of
338 standard normal distribution. Linearity of the quantile-quantile plot implies that residuals
339 are normally distributed as proposed in the Parchment Glutamine Index (PQI) model. With
340 the exception of a few data points on both tails of the quantile-quantile plots, the model
341 fits the deamidation well (Figure 5). The few data points that do not fall onto the quantile-
342 quantile line for peptides COL1 α 2 756-789 and COL1 α 2 535-567 (see Figure 5) is the result of
343 a low signal to noise ratio that affects the correct estimation of q values from the MALDI-TOF
344 spectra.

345 The PQI model predicts the sample level $\log(q)$ value and we therefore argue that the
346 $\exp(\log(q))$ value depicts the overall extent of deamidation in a sample, termed as the Parch-
347 ment Glutamine Index (PQI). From the samples considered in the analysis, PQI predicted
348 from the model ranges from 0.47 to 1.26 with 54% of the values above 1, although theoret-
349 ically the full PQI range is from 0 to 1. A low value of PQI implies more liming and hence low
350 quality of parchment while a value of 1 indicates no deamidation. The model generates some
351 PQI values greater than 1 due to the problem of accurate baseline correction. A histogram
352 of predicted PQI values are shown in Supplementary figure 2.

353 From the PQI model, we estimated peptide level fixed effects and sample level random
354 effects. Whilst the fixed effect is the mean $\log(q)$ of each peptide, the random effect $Y(s)$ is
355 the predicted overall deamidation level in a sample, PQI (see Section 4.4.1). A few q values
356 for the peptides COL1 α 2 756-789 and COL1 α 2 535-567 were not fitted well in the PQI model
357 implying inaccurate estimates from spectral peaks with low signal to noise ratio. Relative to

358 COL1 α 1 508-519, COL1 α 1 375-396 displayed higher rates of deamidation where as COL1 α 1
359 270-291 displayed lowest rate (see Table 3).

360 **5.2 Applications of PQI**

361 As an illustration of the application of the PQI model we explore levels of deamidation from
362 a collection of manuscripts from the library at Orval Abbey, Belgium[Ruffini-Ronzani et al.,
363 2021] by comparing PQI values with species, thickness, typology, and production period as
364 shown in Figure 6.

365 **PQI vs species:** PQI varies with species, parchment produced from calf has higher PQI
366 values, than those produced from sheep or goat (Figure 6a). Goat skin parchments had the
367 lowest PQI, suggesting that they were the most aggressively limed. We also observe the
368 highest PQI values in calfskin used for Bible, and we speculate that this would probably have
369 been perceived as of the best quality. Law and science texts tended to use the lowest quality
370 parchment, although within each group of texts there was considerable variation (Figure 6b).

371 **PQI vs parchment thickness:** Sheep showed the widest range of values, and goat had
372 the lowest PQI values (most deamidated). Estimated thickness suggests that the (small num-
373 ber of) very finest parchment (Thickness index 1) are not of the best quality, an unexpected
374 finding which should be explored further. There is nevertheless a gradual fall in PQI in the
375 next three thickness groups as might be expected, with the greatest levels of deamidation in
376 the coarsest membranes as shown in Figure 6d.

377 **PQI vs time:** A temporal comparison of parchment production from the 9th century
378 until the 17th century reveals the highest PQI values occurred during the “golden age” of
379 the Orval scriptorium (first half of the 13th century), presumably before the disastrous fire
380 of 1252 (see Figure 6c).

381 **CONCLUSION**

382 The PQI model allows us to reliably estimate the quality of parchment production by de-
383 riving an index which combines the extent of deamidation of seven tryptic peptide markers

384 from MALDI-TOF analysis (also known as ZooMS). It uses a three step workflow, the pre-
385 processing of spectra for optimal assessment of each mass envelope, estimating deamidation
386 levels in peptides using weighted least square linear regression, and finally, predicting the
387 overall deamidation level in a sample using a linear mixed effect model. Each step is coded
388 in R as a package `MALDIpqi()`, enabling high throughput analysis of large datasets.

389 We applied the workflow to 3714 MALDI-TOF spectra from parchments in the library of
390 the Orval Abbey and were able to observe a number of patterns. There is a large variation in
391 PQI between membranes but some patterns are evident. Coarser membranes are more heavily
392 limed than thinner folia, and calfskin is more gently processed than sheep and goatskin. Both
393 of these would be anticipated based upon our knowledge of parchment production, although
394 we were surprised by the low PQI values of goatskin, which is typically less fatty than
395 sheepskin and therefore does not require such long exposure to saponify and hence remove
396 lipids. More subtle observations are also apparent at Orval Abbey; texts acquired after the
397 fire of 1252 are on average worse than those acquired during the so-called golden age which
398 preceded it.

399 In addition to this biocodological application of PQI, livestock collagen is widely used
400 in the food industry and biomedicine. Therefore the developed three step workflow offers a
401 simple method to assess levels of Gln deamidation of processed collagen.

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






















Peptide	m/z	nQ	Sequence	<i>Bos taurus</i>  <i>Ovis aries</i>  <i>Capra hircus</i> 
COL1 α 1 508-519	1105.58	1	GVQGGPPGAGPR (1 Hyp)	  
COL1 α 1 270-291	2019.95	1	GEPGPTGIQGGPPGAGEEGKR (2 Hyp)	  
COL1 α 1 375-396	2040.97	1	TGPPGAGQDGRPGPPGPPGAR (3 Hyp)	  
COL1 α 1 934-963	2689.25	2	GFSGLQGGPPGPPGSPGEGQGPSGASGPAGPR (2 Hyp)	  
COL1 α 2 756-789	3033.50	1	GPSGEPGTAGPPGTPGPQGLLGAPGFLGLPGSR (5 Hyp)	 
COL1 α 2 535-567	3093.48	1	GPSGEPGTAGPPGTPGPQGFLGPPGFLGLPGSR (5 Hyp)	 
COL1 α 1 9-42	3084.42	2	GLPGGPGAPGPQGFQGGPPGEPGEPGASGPMGPR (5 Hyp)	  
COL1 α 1 9-42	3116.40	2	GLPGGPGAPGPQGFQGGPPGEPGEPGASGPMGPR (7 Hyp?)	  

Table 1: List of peptides used in the analysis, using the Brown et al. (2020) nomenclature for ZooMS peptides. Sequences for each mass were inferred from Mascot analysis of parchment datasets (SF and JW personal communication). Masses consistent with typical hydroxylation patterns of collagen except where indicated by “?”.

Variable	Usage	Type	Range
Sample (S)	Random effect	Categorical	Levels: $n_S = 3714$
Technical replicate (R)	Random effect	Categorical	Levels: $n_R = 3$
Peptides (P)	Fixed effect	Categorical	Levels: $n_P = 8$
$\log(q)$	Response variable	Continuous	$[-5.50:0.84]$
Reliability	Weight	Continuous	$[0:436634.4]$

Table 2: Summary of the dataset

Peptide	1st quartile of q	Median q	3rd quartile of q	$\exp(\hat{\theta})$	Relative rates of deamidation
COL1 α 1 508-519	1.01	1.08	1.15	1.07	1.00
COL1 α 1 270-291	0.93	1.06	1.14	1.03	6.56
COL1 α 1 375-396	0.32	0.49	0.78	0.46	15.38
COL1 α 1 934-963	0.82	1.00	1.18	0.98	5.71
COL1 α 2 756-789	0.72	0.89	1.08	0.85	9.76
COL1 α 2 535-567	0.64	0.78	0.93	0.74	10.34
COL1 α 1 9-42	0.81	0.92	0.96	0.91	9.66
COL1 α 1 9-42*	0.63	0.79	0.94	0.74	9.41

Table 3: Summary of the extent of deamidation in peptides and Restricted Maximum Likelihood estimates for fixed effects and relative rates of deamidation. Herein, q is the extent of deamidation in the peptides (from weighted least square linear regression) and $\exp(\hat{\theta})$ is the fixed effect estimates (from the PQI model).

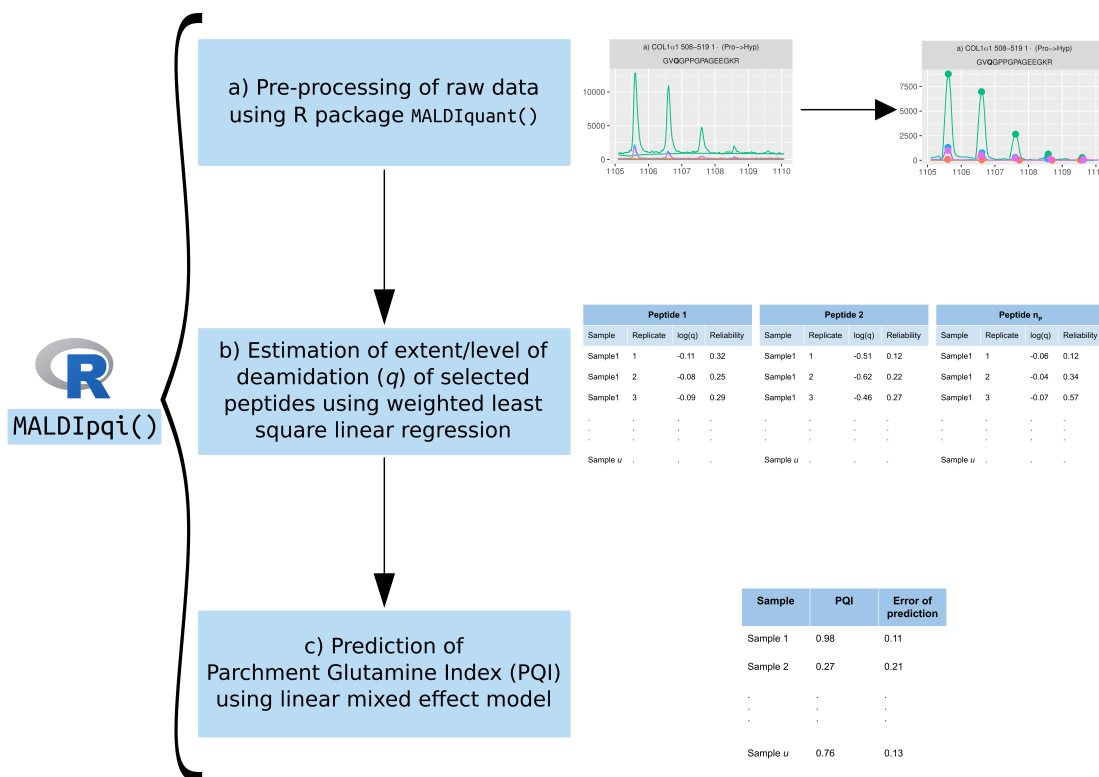


Figure 1: Summary of the workflow developed as an R package MALDIpqi. MALDIpqi consists of three steps, a) pre-processing of MALDI-TOF mass spectra, b) estimation of q of selected peptides, and c) prediction of PQI.

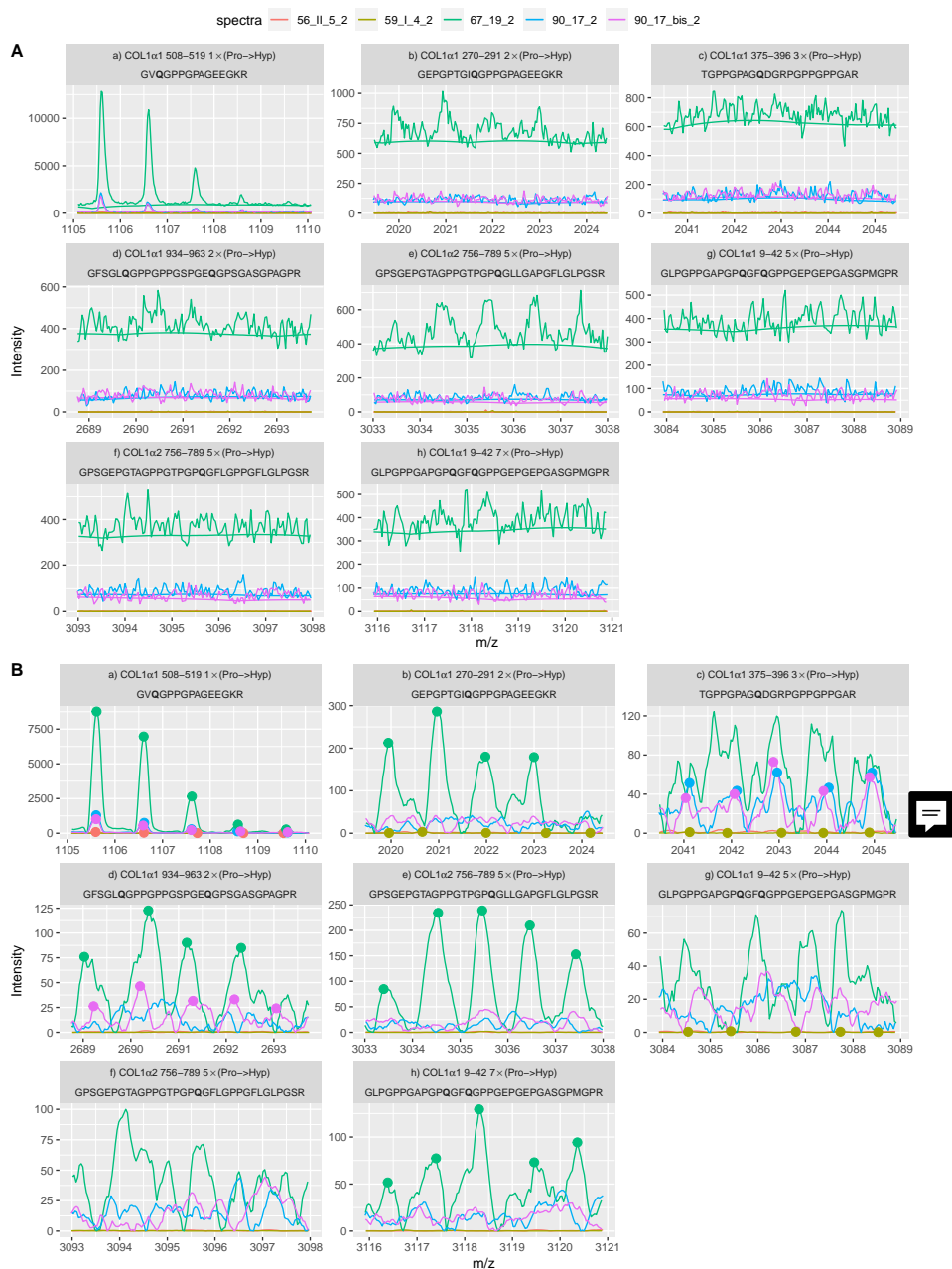


Figure 2: Illustration of overlapping isotopic distribution (up to 6 peaks) of deamidated and non-deamidated fraction of peptides used in the model before (a), and after preprocessing (b). We show the baseline estimated on the smoothed spectra and the peaks that are detected after the preprocessing step 3). Note the variation in intensity and the difference in the signal to noise ratio of peaks for each peptide. Whereas there is a clear distinction of individual peaks (hence, high signal to noise ratio) for COL1α1 508-519, peak distinction becomes complex for COL1α1 9-42 or COL1α2 756-789 due to the noisy spectra (hence, less signal to noise ratio). Five randomly selected samples are shown here.

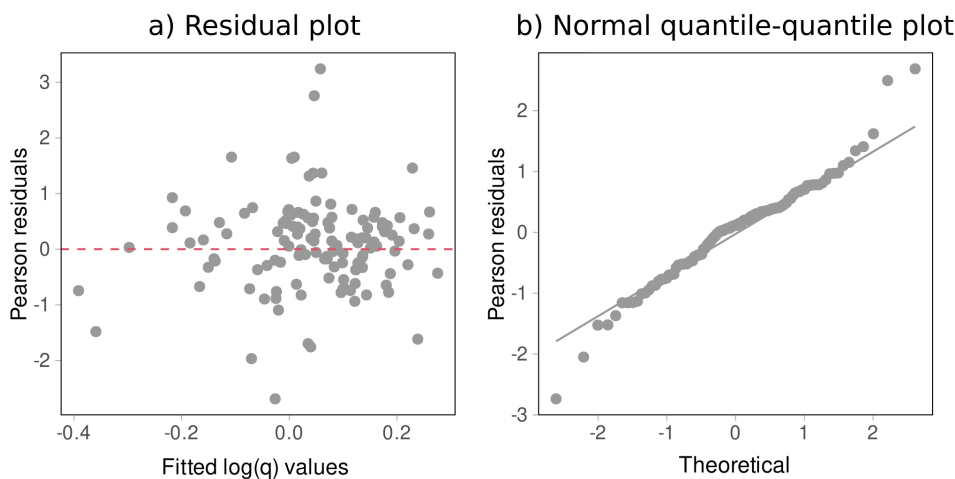


Figure 3: Diagnostic plots for PQI model fitting for COL1 α 1 508-519 indicating a valid statistical model. a) Residual plot between fitted $\log(q)$ values and Pearson residuals, and b) quantile-quantile plot of residuals wherein the grey line indicates the 1-1 line. Both diagnostic plots indicates that the PQI model is valid except slightly too heavy tails in the normal distribution. 200 randomly selected data points are shown in each plot.

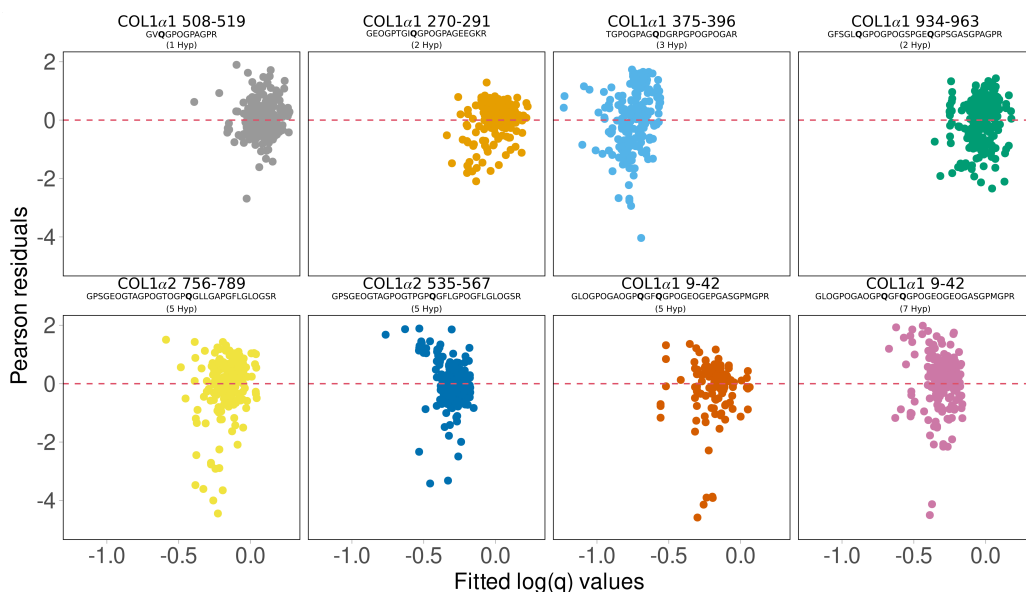


Figure 4: Residual plots between fitted values and Pearson residuals for a) COL1 α 1 508-519, b) COL1 α 1 270-291, c) COL1 α 1 375-396, d) COL1 α 1 934-963, e) COL1 α 2 756-789, f) COL1 α 2 535-567, g) COL1 α 1 9-42 (5 Pro \rightarrow Hyp), and h) COL1 α 1 9-42 (7 Pro \rightarrow Hyp), explores the model fitting quality. Random distribution of standardised residuals around 0 within ± 2 suggests that the proposed linear mixed effect model fits well. However, there are a few badly modelled q values for some of the peptides. 200 randomly selected data points are shown in each plot.

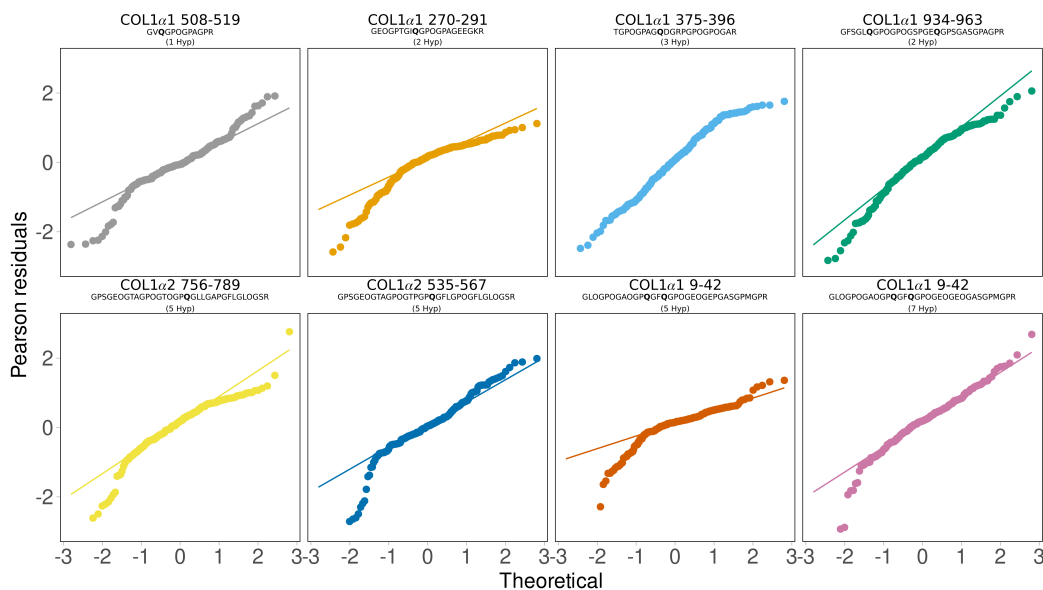


Figure 5: Normal quantile-quantile plots of Pearson residuals for the model fit for a) COL1 α 1 508-519, b) COL1 α 1 270-291, c) COL1 α 1 375-396, d) COL1 α 1 934-963, e) COL1 α 2 756-789, f) COL1 α 2 535-567, g) COL1 α 1 9-42 (5 Pro \rightarrow Hyp), and h) COL1 α 1 9-42 (7 Pro \rightarrow Hyp). Except a few deviations from the inserted 1-1 lines, in particularly at the tails for some of the peptides, the quantile-quantile plots indicates normality of the residuals as proposed by the PQI model. 200 randomly selected data points are shown in each plot.

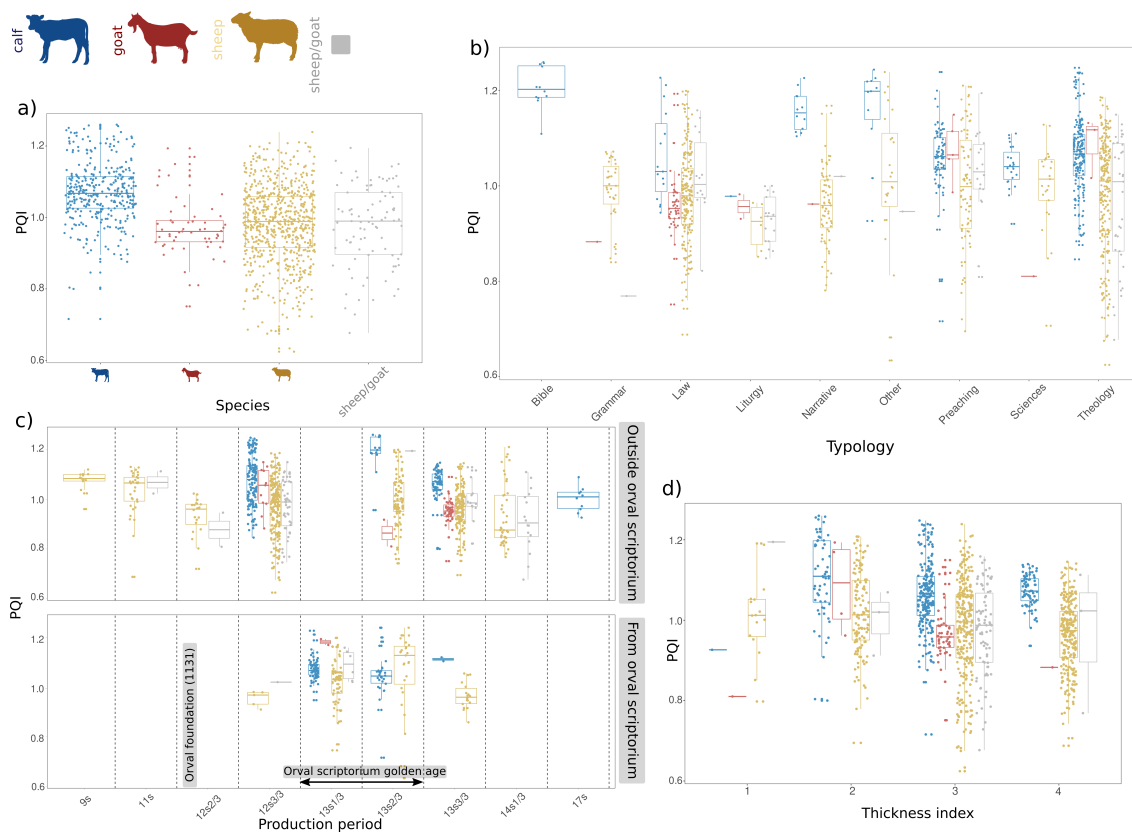


Figure 6: Plots depicting applications of PQI: a) Comparison of PQI against different species used for the production of parchment depicting that manuscripts made out of calfskin were of better quality than the ones made with sheepskin or goatskin. b) Comparison of PQI against different typology the parchments were used for. Biblical manuscripts were written on calfskin, having the highest PQI, which is in accordance with the findings in (Ruffini-Ronzani et al., 2021). Sheepskin was commonly used to produce grammar and theology texts with an intermediate deamidation index. c) Comparison of PQI against production period for parchment locally produced in Orval scriptorium (bottom panel) and for imported parchments (top panel) starting from 9th century until 17th century. The timeline is organised by thirds of a century (early, mid, and late). Orval scriptorium was founded in the early 12th century. The use of calfskin to produce parchments remained constant during the “golden age”(first third and second third of the 13th century) of the scriptorium. d) Comparison of PQI against the thickness indices of codicological units. The thickness was determined depending on the number of folios in the codicological unit (Thickness index; 1 = less than 10 folia, 2 = 11-100 folia, 3 = 101-200 folia, 4 = greater than 200 folia.). (Icons of calf, goat, and sheep created with BioRender.com)